

## Final Exam

### Exercise 1: (13 pts)

Answer with True or False (and correct the statement if it is false):

- 1) Electrostatics studies moving point charges.
- 2) The unit of the electric field is  $V \cdot m$ .
- 3) The unit of the Coulomb force is  $N \cdot C^{-1}$ .
- 4) Electrostatic interaction can be repulsive.
- 5) Electrostatic interaction can be attractive.
- 6) The force  $\vec{F}$  acting on a particle of charge  $q$  placed at a point  $A$  in an electrostatic field is related to the field  $\vec{E}$  by the relation:  $\vec{E} = q\vec{F}$
- 7) In an electric dipole, the direction of the electric field goes from the positive charge (+) to the negative charge (-).
- 8) The displacement vector in cylindrical coordinates is:  $d\vec{l} = dr\vec{u}_r + d\theta\vec{u}_\theta + dz\vec{k}$

Choose or circle the correct answer:

- 9) The force between two like charges  $q_1$  and  $q_2$  is:  
a) Repulsive if:  $q_1 \times q_2 > 0$       b) Zero if the distance between  $q_1$  and  $q_2$  is zero      c) Attractive if  $q_1 \times q_2 < 0$

10) What is an equipotential surface?

- a) A surface where the electric field is zero everywhere.      b) A surface where the electric potential is constant.  
c) A surface where charges can move freely.      d) A surface where the electric potential increases linearly.

11) Which of the following is the correct expression for the scalar Laplacian :

- a)  $\nabla f = \frac{\partial f}{\partial x} + \frac{\partial f}{\partial y} + \frac{\partial f}{\partial z}$       b)  $\nabla \cdot f = \frac{\partial f}{\partial x} + \frac{\partial f}{\partial y} + \frac{\partial f}{\partial z}$       c)  $\Delta f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2} + \frac{\partial^2 f}{\partial z^2}$       d)  $\nabla \times f = 0$

12) Green-Ostrogradsky Theorem:

- a)  $\oint \vec{A} \cdot d\vec{S} = \oint \text{rot} \vec{A} \cdot d\vec{S}$       b)  $\oint \vec{A} \cdot d\vec{S} = \oint \text{grad} \vec{A} \cdot dV$       c)  $\oint \vec{A} \cdot d\vec{S} = \oint \text{div} \vec{A} \cdot dV$

13) The electric dipole moment is defined as:

- a)  $\vec{p} = q \cdot \vec{d}$       b)  $\vec{p} = \epsilon_0 \cdot \vec{E}$       c)  $\vec{p} = q \cdot \vec{r}^2$       d)  $\vec{p} = \frac{q}{d}$

### Exercise 2: (3 pts) Calculate the following quantities:

$$f(x, y, z) = 3xyz^3 - 2y \quad \vec{A} = r.z\vec{u}_r + r.\cos\theta\vec{u}_\theta + r.z^2\vec{u}_z \quad \vec{B} = r\vec{u}_r + r.\cos\theta.\sin\phi\vec{u}_\theta + r.\cos\phi\vec{u}_\phi$$

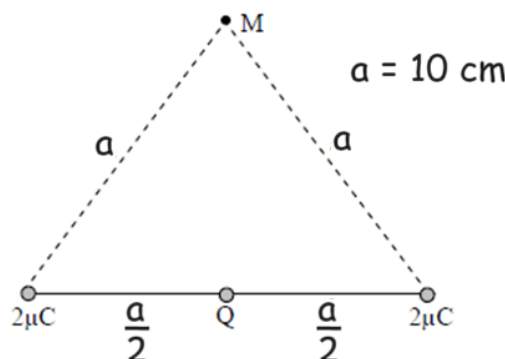
$$\text{grad} f = \dots\dots\dots$$

$$\text{div} \vec{A} = \dots\dots\dots$$

$$\text{rot} \vec{B} = \dots\dots\dots$$

### Exercise 3: (4 pts) Three point charges are aligned as shown in the figure.

1. Calculi the result Force at the charge Q ?
2. Calculate the value of charge Q so that the resulting electric field at point M is zero.
3. Calculate the electric potential at point M.



$$K = 8,987 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$$