



### Third-Semester Examination in Statistics 03, Ordinary session

#### Academic Year 2025–2026

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#### EX:01: (6.5 Points)

A bookstore receives customers according to a Poisson process at an average rate of **8 customers per hour**. Assume the number of customers arriving follows a Poisson distribution.

1. Compute the probability that **exactly 5 customers** arrive in the next hour.
2. What is the probability that **at most 3 customers** arrive in the next hour?
3. What is the probability that **no customers** arrive in the next **30 minutes**?
4. Find the **mean and variance** of the number of customers arriving in **90 minutes**.

#### Exo:02: (6.5 Points)

A manufacturing process for electronic components occasionally produces a defective item due to a rare but persistent flaw. From quality control history, about 8% of components produced are defective.

Let **X be the number of components tested until the first defective is found**, calculate the following

$$P(X = 3), \quad P(X \geq 5), \quad E(X), \quad Var(X)$$

2- calculate  $P(X \geq 8/X > 4)$  and explain how this illustrates the **memoryless property** of the geometric distribution.

#### Ex:03: (3 Points)

The lifetime **X** (in years) of a fuse in a backup power unit follows an exponential distribution with rate parameter  $\lambda = 2$

1. What is the probability that the fuse lasts at least 1 year without failing?
2. What is the probability that the fuse fails within the first 0.5 years?
3. Find the median lifetime of the fuse

**Exo: 04: (4 Points)**

A random sample of size  $n=21$  is drawn from a normal distribution with unknown mean  $u$  and unknown standard deviation  $s$ . Let  $\bar{x}$  denote the sample mean and  $s$  the sample standard deviation. Consider the statistic

$$T = \frac{\bar{x} - u}{s/\sqrt{n}}$$

1. **Identify the sampling distribution** of  $T$  and its degrees of freedom
2. **Compute**  $P(T > 2.845)$
3. **Determine** the symmetric interval  $(-t^*, t^*)$  such that  $P(-t^* < T < t^*) = 0.99$
4. **Find the value**  $t$  such that  $P(T < t) = 0.95$

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